## SEKOLAH BUKIT SION

IGCSE Mock Examination 2021

## STUDENT

 NAME
## EXAM

 NUMBER $\square$CLASS


## 0606 ADDITIONAL MATHEMATICS (PAPER 1)

Year 10
10 April 2021
1 hour 30 minutes
Additional Materials:

- Scientific Calculator
- Ruler
- Graphing Paper


## READ THESE INSTRUCTIONS FIRST

Write your name, exam number and grade on all the work you hand in.
Write in dark blue or black pen.
Use an HB pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.

Answer all questions.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question. The total of the marks for this paper is 60.

Score :

This document consists of $\mathbf{1 1}$ printed pages including this page.
(a) Sketch the graph of $y=|4 x-2|$ on the axes below, showing the coordinates of the points where the graph meets the axes.


2 Find the equation of the normal to the curve $y=\sqrt{8 x+5}$ at the point where $x=\frac{1}{2}$, giving your answer in the form of $a x+b y+c=0$, where $a, b$ and $c$ are integers.

| Question | Answer | Marks | AO Element | Notes | Guidance | Clos |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\text { M1 } \frac{\mathrm{d} y}{\mathrm{~d} x}=k(8 x+5)^{-\frac{1}{2}}$ $\text { A1 } \frac{\mathrm{d} y}{\mathrm{~d} x}=4(8 x+5)^{-\frac{1}{2}}$ <br> B1 When $x=\frac{1}{2}, y=3$ <br> M1 Normal: $y-3=-\frac{3}{4}\left(x-\frac{1}{2}\right)$ <br> A1 $6 x+8 y-27=0$ | 5 |  | For attempt to differentiate, must be in the form $k(8 x+5)^{-\frac{1}{2}}$ <br> For attempt at the normal when $x=\frac{1}{2}$, using correct process for their $\frac{\mathrm{d} y}{\mathrm{~d} x}$ and their y . |  |  |
| [Total: 5] |  |  |  |  |  |  |

3 Find the values of $k$ for which the line $y=k x-3$ and the curve $y=2 x^{2}+3 x+k$ do not intersect. [5]

| Question | Answer | Marks | AO Element | Notes | Guidance |
| :---: | :--- | :---: | :---: | :--- | :--- |
| 1 | M1 $2 x^{2}+3 x+k=k x-3$ | $\mathbf{5}$ |  | For an attempt to equate <br> and simplify to a 3 term <br> quadratic equation, allow <br> an error in one term |  |
|  | A1 $2 x^{2}+(3-k) x+(k+3)=0$ |  |  |  |  |
| M1 $(3-k)^{2}-4 \times 2 \times(k+3)$ |  | For attempt to use the <br> discriminant, allow <br> previous error leading to <br> a quadratic equation in <br> terms of $k$ <br> For critical values |  |  |  |


| Question | Answer | Marks | AO Element | Notes | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | M1 $6 x^{2}+7 x-20[* 0]$ <br> A1 Critical values $\frac{4}{3},-\frac{5}{2}$ <br> A1 $x \leqslant-\frac{5}{2}$ or $x \geqslant \frac{4}{3}$ final answer | 3 |  | where * may be any inequality sign or $=$ <br> FT their critical values using outside regions |  |
| [Total: 3] |  |  |  |  |  |

5 The functions $f$ and $g$ are defined for real values of $x$ by
$\mathrm{f}(x)=\sqrt{x-1}-3$ for $x>1$,
$\mathrm{g}(x)=\frac{x-2}{2 x-3}$ for $x>2$.
(a) Find $g f(37)$.
(b) Find an expression for $\mathrm{f}^{-1}(x)$.
(c) Find an expression for $\mathrm{g}^{-1}(x)$.

| Question | Answer | Marks | AO Element | Notes | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1(a) | $\begin{aligned} & \mathrm{f}(37)=3 \text { or } \\ & \mathrm{gf}(x)=\frac{\sqrt{x-1}-3-2}{2(\sqrt{x-1}-3)-3} \end{aligned}$ | B1 |  |  |  |
|  | $\operatorname{gf}(37)=\frac{3-2}{6-3}=\frac{1}{3}$ | B1 |  |  |  |
| 1(b) | $y=\sqrt{x-1}-3 \rightarrow(y+3)^{2}=x-1$ | M1 |  | Rearrange and square in any order |  |
|  | $(x+3)^{2}+1=\mathrm{f}^{-1}(x)$ oe isw | A1 |  | Interchange $x$ and $y$ and complete |  |
| 1(c) | $\begin{aligned} & y=\frac{x-2}{2 x-3} \\ & 2 x y-3 y=x-2 \rightarrow 2 x y-x=3 y \end{aligned}$ | M1 |  | Multiply and collect like terms |  |
|  | $\frac{3 x-2}{2 x-1}=\mathrm{g}^{-1}(x) \text { oe }$ | A1 |  | Interchange and complete Mark final answer |  |
| [Total: 6] |  |  |  |  |  |

Solve.
(a) $2(5)^{2 z}+5^{z}-1=0$.

| Question | Answer | Marks | AO Element | Notes | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\left(2\left(5^{z}\right)-1\right)\left(5^{z}+1\right)=0$ | M1 |  | M1 for solution of quadratic |  |
|  | leading to $2.5^{z}=1 \quad\left(5^{z}=-1\right)$ | A1 |  | A1 for correct solution |  |
|  | $5^{z}=0.5$ | M1 |  | DM1 for correct attempt to solve $2.5^{z}=k$, where $k$ is positive |  |
|  | $z=\frac{\log 0.5}{\log 5}$ <br> or $z=-0.431$ or better | A1 |  | A1 must have one solution only |  |
| [Total: 4] |  |  |  |  |  |

(b) $1+2 \log _{5} x=\log _{5}(18 x-9)$

| Question | Answer | Marks | AO Element | Notes | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1+2 \log _{5} x=\log _{5}(18 x-9) \\ & \log _{5} 5+\log _{5} x^{2}=\log _{5}(18 x-9) \end{aligned}$ | B2 |  | B1 for dealing with ' 1 ', <br> B1 for dealing with ' 2 ' |  |
|  | $\log _{5} 5 x^{2}=\log _{5}(18 x-9)$ | M1 |  | for a correct use of addition or subtraction of logarithms |  |
|  | $\begin{aligned} & 5 x^{2}=18 x-9 \\ & (5 x-3)(x-3)=0 \end{aligned}$ | M1 |  | DM1 for elimination of logarithms to form a 3 term quadratic and for solution of quadratic |  |
|  | $x=\frac{3}{5}, 3$ | A1 |  | for both $x$ values |  |
| [Total: 5] |  |  |  |  |  |

7 A curve has equation $y=(3 x-5)^{3}-2 x$.
(a) Find $\frac{d y}{d x}$ and $\frac{d^{2} y}{d x^{2}}$.
(b) Find the exact value of the $x$-coordinate of each of the stationary points of the curve.
(c) Use the second derivative test to determine the nature of each of the stationary points.

| Question | Answer | Marks | AO Element | Notes | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1(a) | B2 $9(3 x-5)^{2}-2$ isw <br> B2 $54(3 x-5)^{[1]}$ isw | 4 |  | B1 for $k(3 x-5)^{2} \quad k \neq 9$ <br> seen <br> B1 for $\begin{aligned} & k(3 x-5)^{[1]} \quad k \neq 54 \\ & \text { seen } \end{aligned}$ |  |
| 1(b) | M1 Solves their $9(3 x-5)^{2}-2=0$ A1 $[x=] \frac{5}{3} \pm \frac{\sqrt{2}}{9}$ or exact equivalent | 2 |  |  |  |
| 1(c) | M1 Substitutes their $\frac{5}{3}+\frac{\sqrt{2}}{9}$ or their $\frac{5}{3}-\frac{\sqrt{2}}{9}$ into their $54(3 x-5)^{[1]}$ and considers sign of result <br> A1 When $x=\frac{5}{3}+\frac{\sqrt{2}}{9} \quad \frac{\mathrm{~d}^{2} y}{\mathrm{~d} x^{2}}>0$ so minimum and when $x=\frac{5}{3}-\frac{\sqrt{2}}{9} \quad \frac{\mathrm{~d}^{2} y}{\mathrm{~d} x^{2}}<0$ so maximum | 2 |  |  |  |



The position vectors of points $A$ and $B$ relative to an origin $O$ are $\mathbf{a}$ and $\mathbf{b}$ respectively.
The point $P$ is such that $\overrightarrow{O P}=\mu \overrightarrow{O A}$. The point $Q$ is such that $\overrightarrow{O Q}=\lambda \overrightarrow{O B}$.
The lines $A Q$ and $B P$ intersect at the point $R$.
(a) Express $\overrightarrow{A Q}$ in terms of $\lambda$, $\mathbf{a}$ and $\mathbf{b}$.
(b) Express $\overrightarrow{B P}$ in terms of $\mu$, $\mathbf{a}$ and $\mathbf{b}$.

It is given that $3 \overrightarrow{A R}=\overrightarrow{A Q}$ and $8 \overrightarrow{B R}=7 \overrightarrow{B P}$.
(c) Express $\overrightarrow{O R}$ in terms of $\lambda$, a and $\mathbf{b}$.
(d) Express $\overrightarrow{O R}$ in terms of $\mu$, a and $\mathbf{b}$.
(e) Hence find the value of $\mu$ and $\lambda$.

| Question | Answer | Marks | AO Element | Notes | Guidance | Close |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1(a) | $\overrightarrow{A Q}=\lambda \mathbf{b}-\mathbf{a}$ | B1 |  |  |  |  |
| 1(b) | $\overrightarrow{B P}=\mu \mathbf{a}-\mathbf{b}$ | B1 |  |  |  |  |
| 1(c) | $\begin{aligned} & \overrightarrow{O R}=\mathbf{a}+\frac{1}{3}(\lambda \mathbf{b}-\mathbf{a}) \text { or } \\ & \lambda \mathbf{b}-\frac{2}{3}(\lambda \mathbf{b}-\mathbf{a}) \end{aligned}$ | M1 |  | $\text { for } \mathbf{a}+\frac{1}{3} \text { their (a) }$ |  | Mark schen |
|  | $=\frac{2}{3} \mathbf{a}+\frac{1}{3} \lambda \mathbf{b}$ | A1 |  | Allow unsimplified |  |  |
| 1(d) | $\begin{aligned} & \overrightarrow{O R}=\mathbf{b}+\frac{7}{8}(\mu \mathbf{a}-\mathbf{b}) \text { or } \\ & \mu \mathbf{a}-\frac{1}{8}(\mu \mathbf{a}-\mathbf{b}) \end{aligned}$ | M1 |  | for $\mathbf{b}+\frac{7}{8}$ their (b) |  |  |
|  | $=\frac{1}{8} \mathbf{b}+\frac{7}{8} \mu \mathbf{a}$ | A1 |  | Allow unsimplified |  |  |
| 1(e) | $\frac{2}{3} \mathbf{a}+\frac{1}{3} \lambda \mathbf{b}=\frac{1}{8} \mathbf{b}+\frac{7}{8} \mu \mathbf{a}$ | M1 |  | for equating (c) and (d) and then equating like vectors |  |  |
|  | $\frac{2}{3}=\frac{7}{8} \mu, \mu=\frac{16}{21}$ Allow 0.762 | A1 |  |  |  |  |
|  | $\frac{1}{3} \lambda=\frac{1}{8}, \lambda=\frac{3}{8} \text { Allow } 0.375$ | A1 |  |  |  |  |

## 9 CHOOSE/ANSWER ONLY ONE.

(a) Given that $7^{x} \times 49^{y}=1$ and $5^{5 x} \times 125^{\frac{2 y}{3}}=\frac{1}{25}$, calculate the value of $x$ and $y$.

| Question | Answer | Marks | AO Element | M1 Either $7^{x} \times 7^{2 y}$ or $49^{\frac{x}{2}} \times 49^{y}$ <br> or $5^{5 x} \times 5^{2 y}$ or $25^{\frac{5 x}{2}} \times 25^{y}$ | $\mathbf{5}$ |
| :---: | :--- | :---: | :--- | :--- | :--- |
| 1 | A1 $7^{x} \times 7^{2 y}=7^{0}$ <br> or $49^{\frac{x}{2}} \times 49^{y}=49^{0}$ <br> A1 $5^{5 x} \times 5^{2 y}=5^{-2}$ <br> or $25^{\frac{5 x}{2}} \times 25^{y}=25^{-1}$ <br> M1 leading to $x+2 y=0$ <br> and $5 x+2 y=-2$ | For expressing the terms <br> on the left hand side of <br> either one of the 2 <br> equations in terms of <br> powers of 7, 49, 5 or <br> 25 |  |  |  |
|  |  |  | For attempt to solve two <br> linear equations, with <br> integer coefficients and <br> constants, in terms of $x$ <br> and $y$ |  |  |

(b) Without using a calculator, express $(\sqrt{5}-3)^{2}$ in the form of $p \sqrt{5}+q$, where $p$ and $q$ are integers.

$$
\begin{equation*}
\sqrt{5}+1 \tag{4}
\end{equation*}
$$

| Question | Answer | Marks | AO Element | Notes | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\text { M1 }(\sqrt{5}-3)^{2}=5+9-2(3) \sqrt{5}$ $\text { M1 } \frac{\text { their }(14-6 \sqrt{5})}{\sqrt{5}+1} \times \frac{\sqrt{5}-1}{\sqrt{5}-1}$ <br> M1 $\frac{\text { their }(14 \sqrt{5}-30-14+6 \sqrt{5})}{5-1}$ <br> A1 $5 \sqrt{5}-11$ | 4 |  | Attempts to rationalise or forms a pair of simultaneous equations e.g. $5 p+q=14, p+q=-6$ <br> multiplies out; numerator must have at least 3 terms; condone one sign error in numerator; denominator may be 4 or $5-\sqrt{5}+\sqrt{5}-1$ or solves their simultaneous equations to find one unknown $\text { or } p=5, q=-11$ |  |
|  |  |  |  |  | [Total: 4] |

10 The polynomial $\mathrm{p}(x)=(2 x-1)(x+k)-12$, where $k$ is a constant.
(a) Write down the value of $\mathrm{p}(-k)$.
(b) When $\mathrm{p}(x)$ is divided by $(x+3)$, the remainder is 23 .

Find the value of $k$.
(c) Using your value of $k$ in part (b), show that the equation $\mathrm{p}(x)=-25$ has no real solutions.

| Question | Answer | Marks | AO Element | Notes | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1(a) | B1-12 | 1 |  |  |  |
| 1(b) | M1 $(2 \times-3-1)(k-3)-12=23 \text { oe }$ or $\begin{array}{r} 2(-3)^{2}+(2 k-1)(-3)-k-12 \\ =23 \end{array}$ $\mathbf{A 1} k=-2$ | 2 |  |  |  |
| 1(c) | $\begin{aligned} & \text { M1 }(2 x-1)(x-2)-12=-25 \\ & 2 x^{2}-5 x+15=0 \end{aligned}$ <br> M1 Discriminant: $\begin{aligned} & 25-(4 \times 2 \times 15) \\ & =-95 \end{aligned}$ <br> A1 which is $<0$ so no real solutions | 3 |  | expansion and simplification to a 3 term quadratic equation equated to zero, using their $k$. <br> using discriminant for their three term quadratic equation <br> cao for correct discriminant and correct conclusion |  |
|  |  |  |  |  | [Total: 6] |

- END OF EXAMINATION -

